

A Biologically Plausible Learning Algorithm for Neural Networks

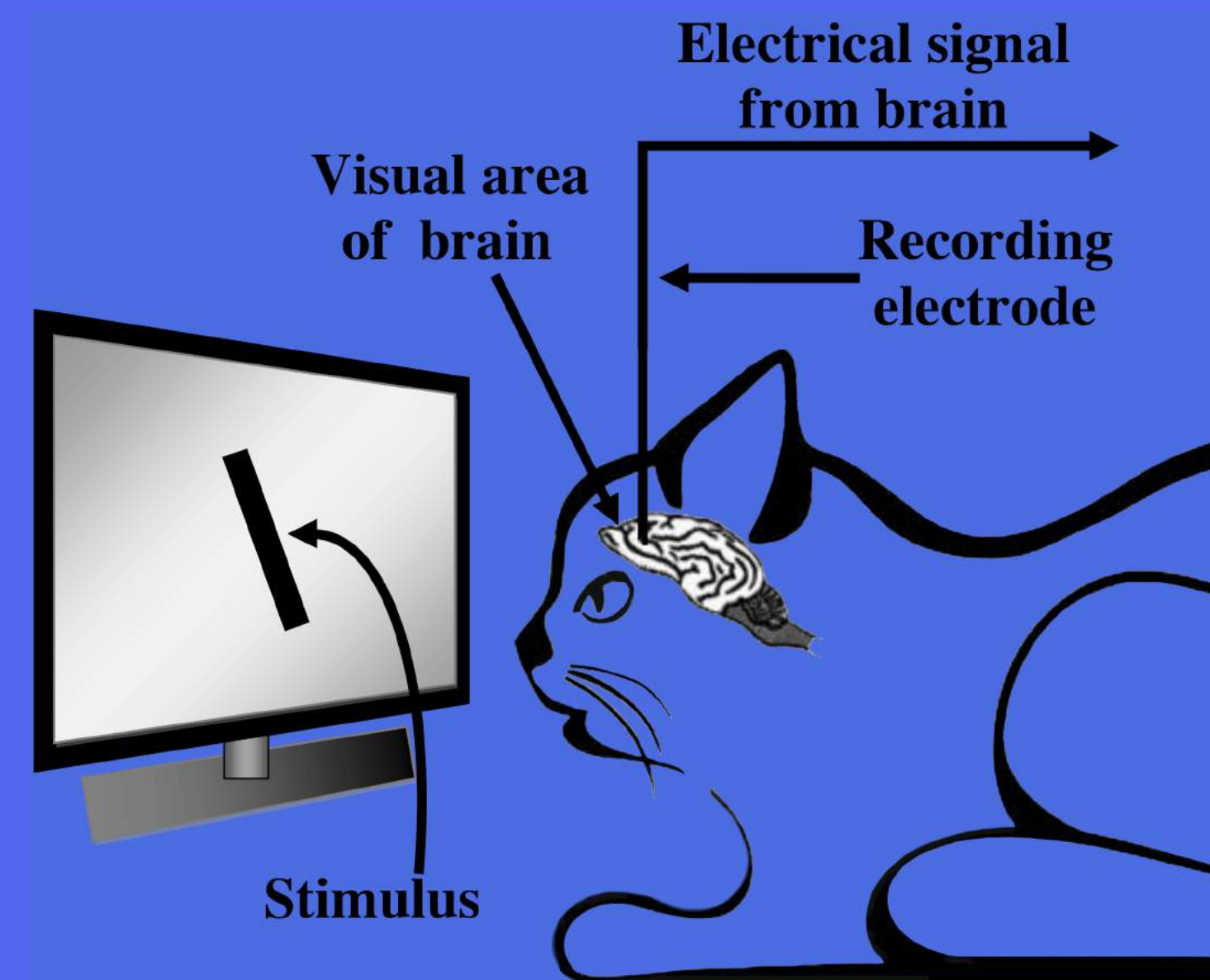
Dmitry Krotov
MIT-IBM Watson AI Lab
IBM Research

Does brain do deep learning?

- Architectural similarity between CNNs and visual cortex
- Similarity of the receptive fields of CNNs and direction selective cells

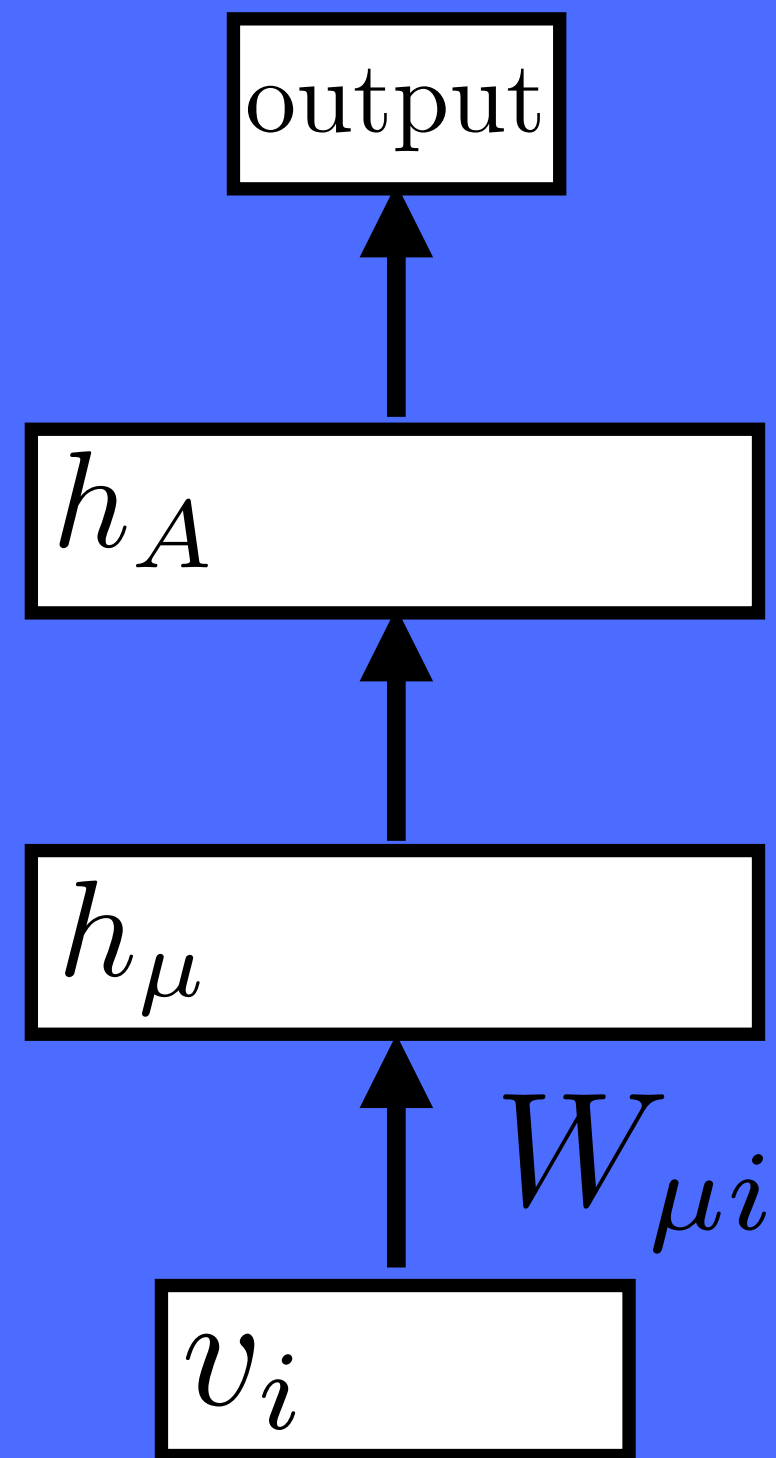


Zeiler and Fergus, 2014



Hubel Wiesel, 1959

Does brain do backpropagation?

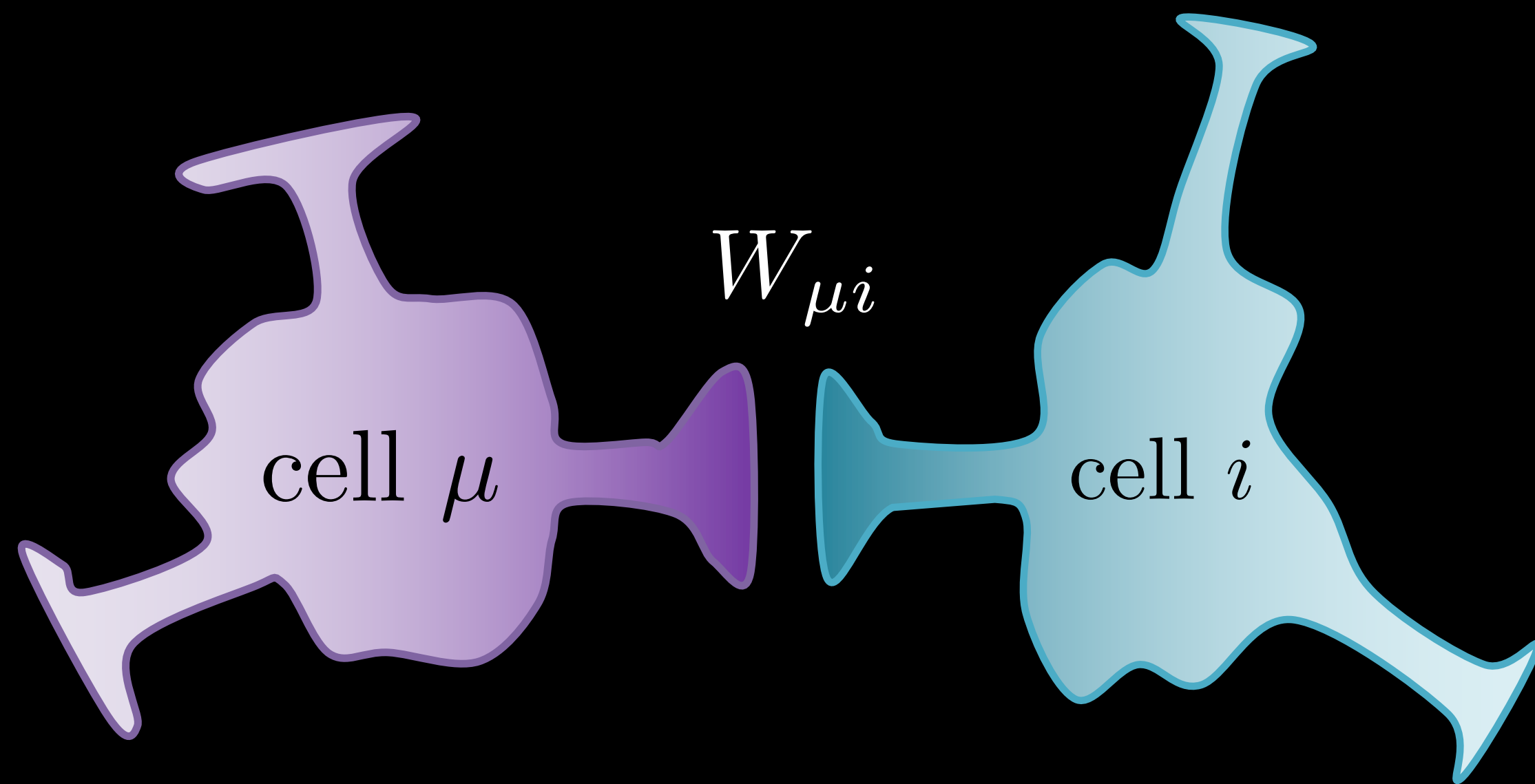


$$L = \sum_{\text{data}} (\text{output} - \text{target})^2$$

$$\Delta W_{\mu i} = -\varepsilon \frac{\partial L}{\partial W_{\mu i}} = \varepsilon \left(\dots \right)$$

The update rule is non-local

Biological plasticity rules



$$\Delta W_{\mu i} = f(I_{\mu}, I_i)$$

I_{μ} – information available to cell μ

I_i – information available to cell i

The update rule is local

Supervised backpropagation learning versus biological learning



VS.



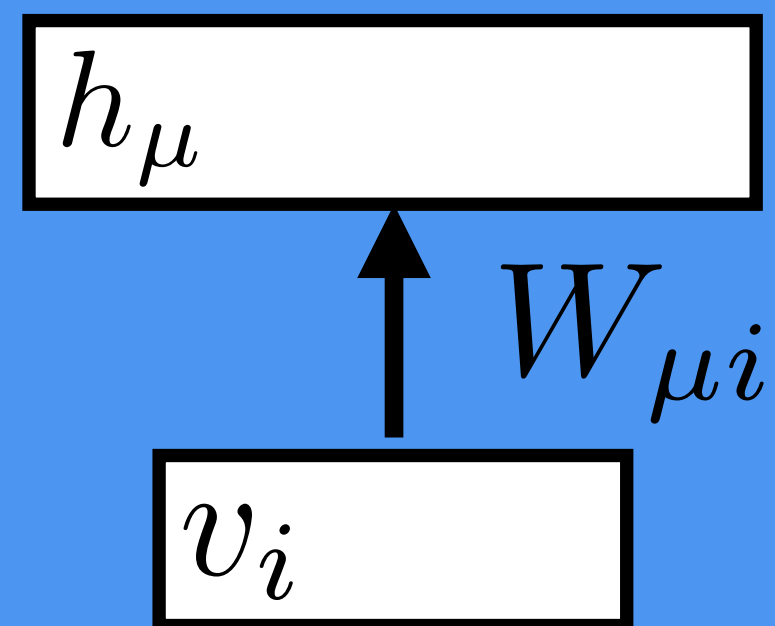
heavily supervised
greedy on labeled data

mostly unsupervised
very few labeled examples

Main question:

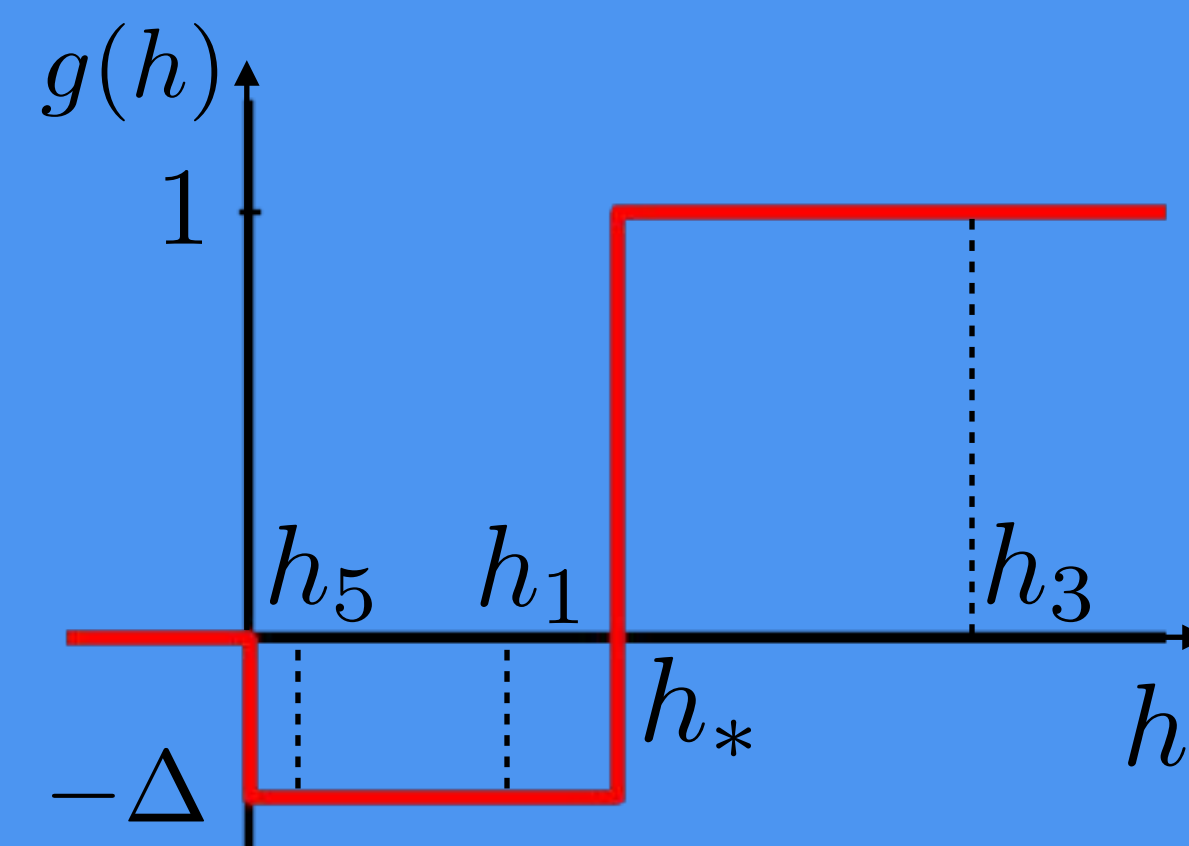
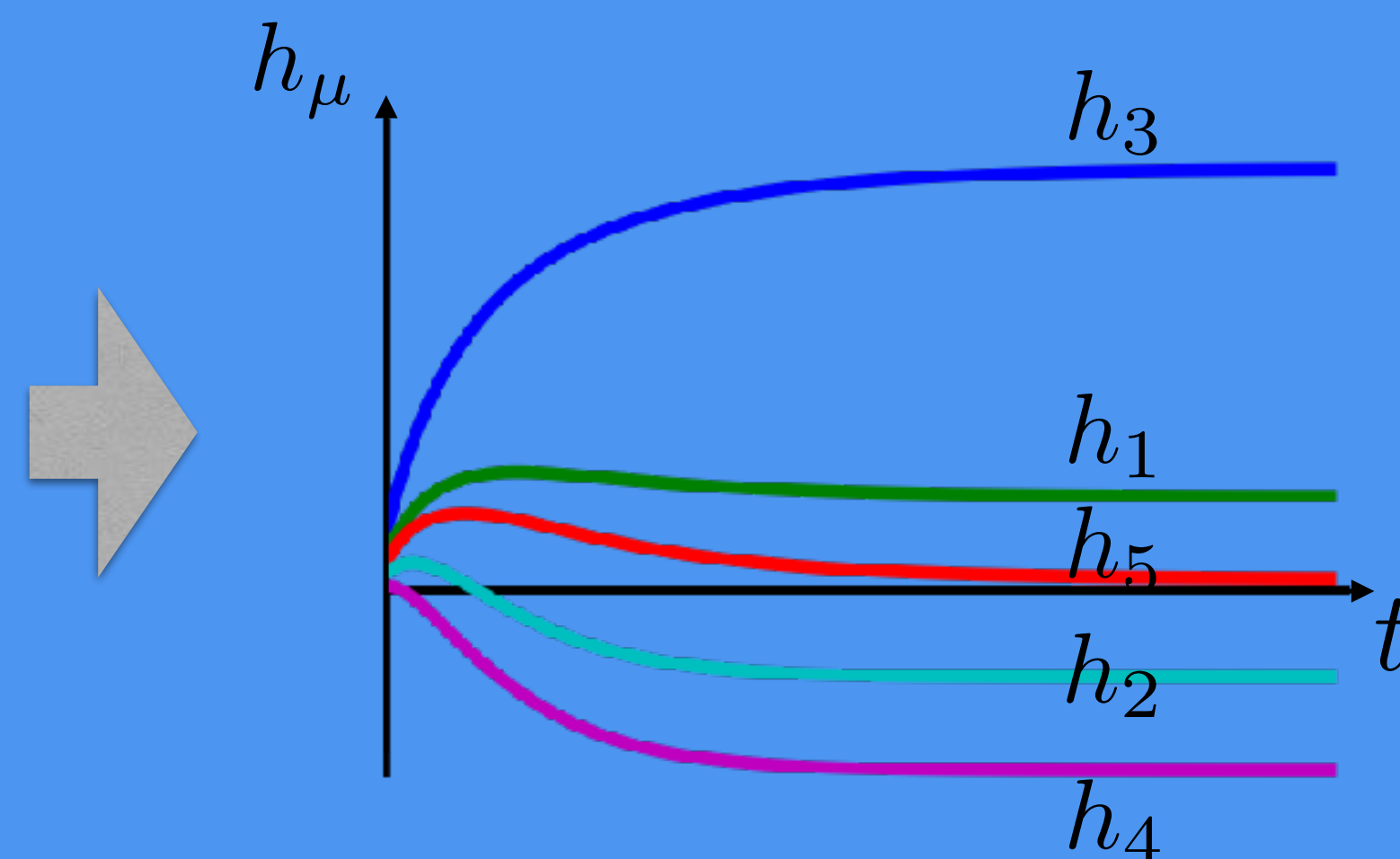
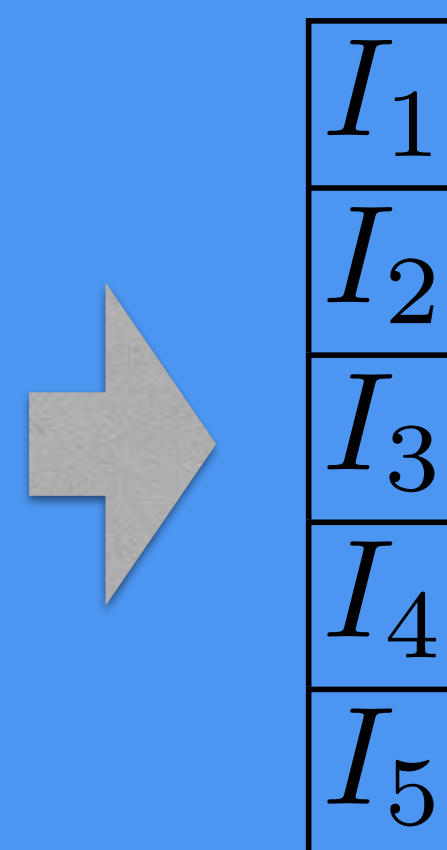
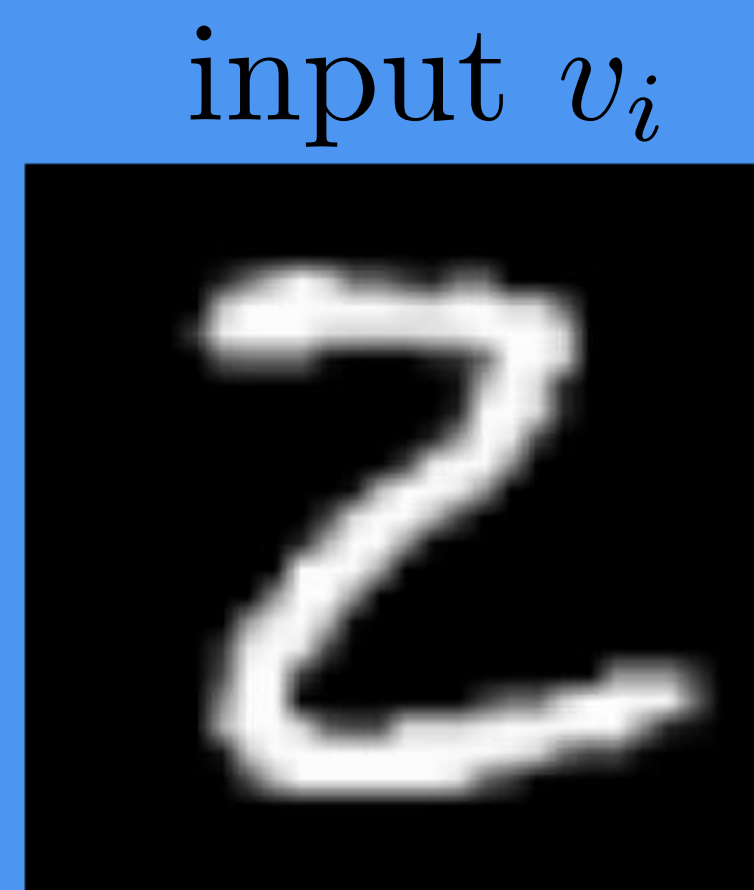
Given unsupervised aspect of learning and locality of synaptic plasticity rules, can we engineer a learning algorithm that leads to a good generalization performance?

Learning algorithm



$$\tau \frac{dh_\mu}{dt} = I_\mu - w_{\text{inh}} \sum_{\nu \neq \mu} r(h_\nu) - h_\mu$$

$$I_\mu = \sum_{i=1}^N W_{\mu i} v_i$$



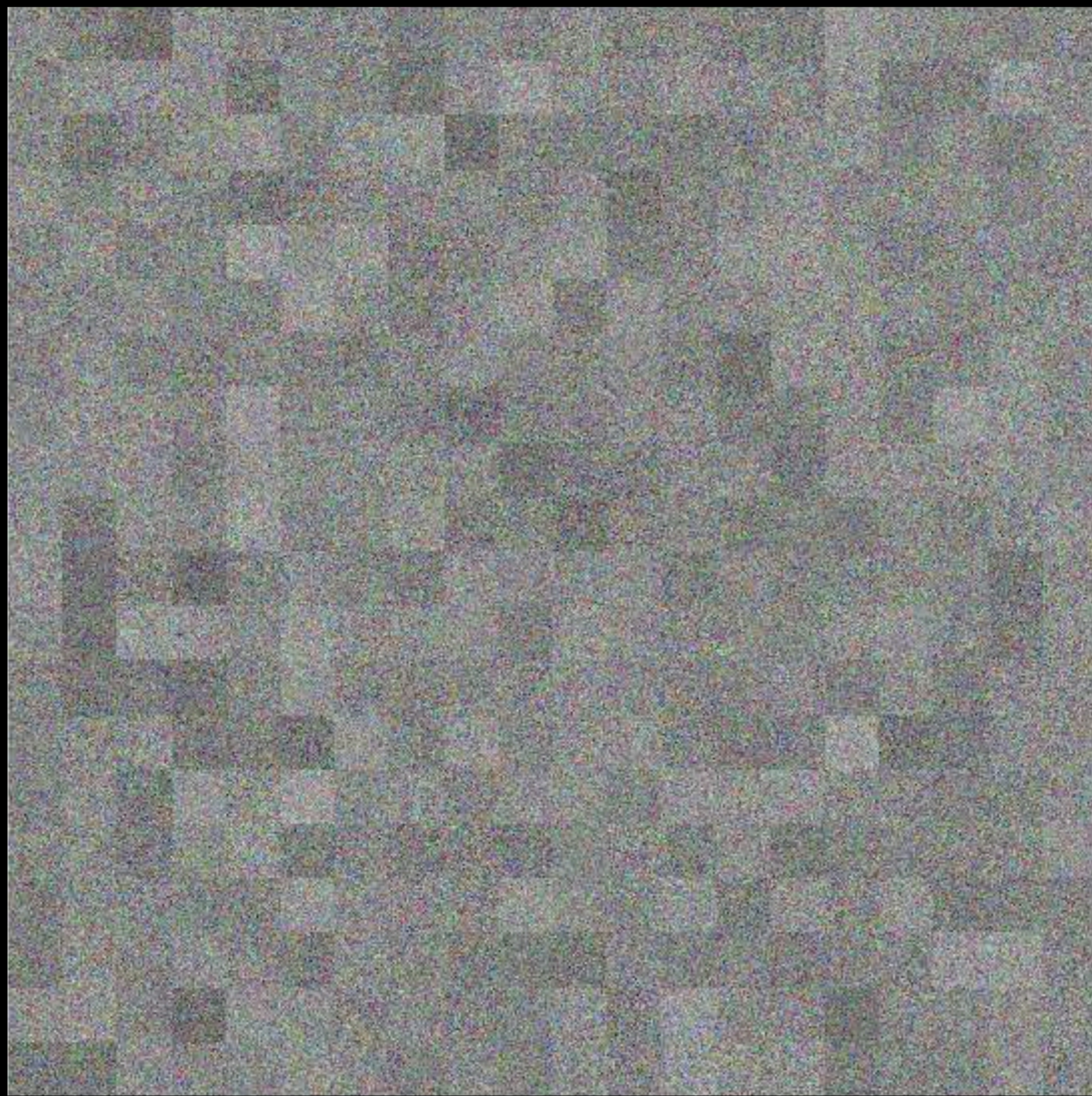
$$\Delta W_{\mu i} \sim g(h_\mu) v_i \quad \text{Hebbian learning}$$

Synaptic plasticity rule

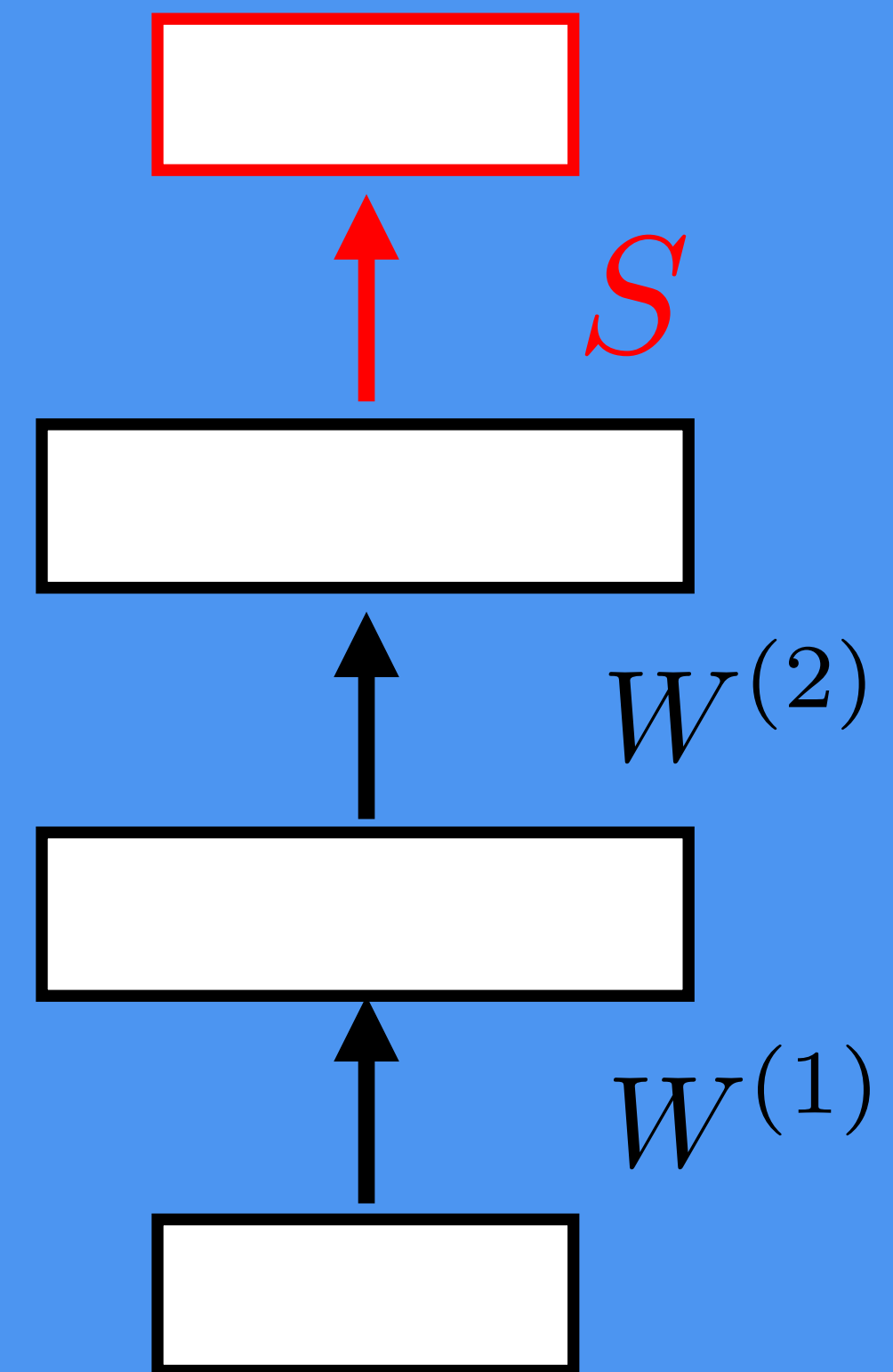
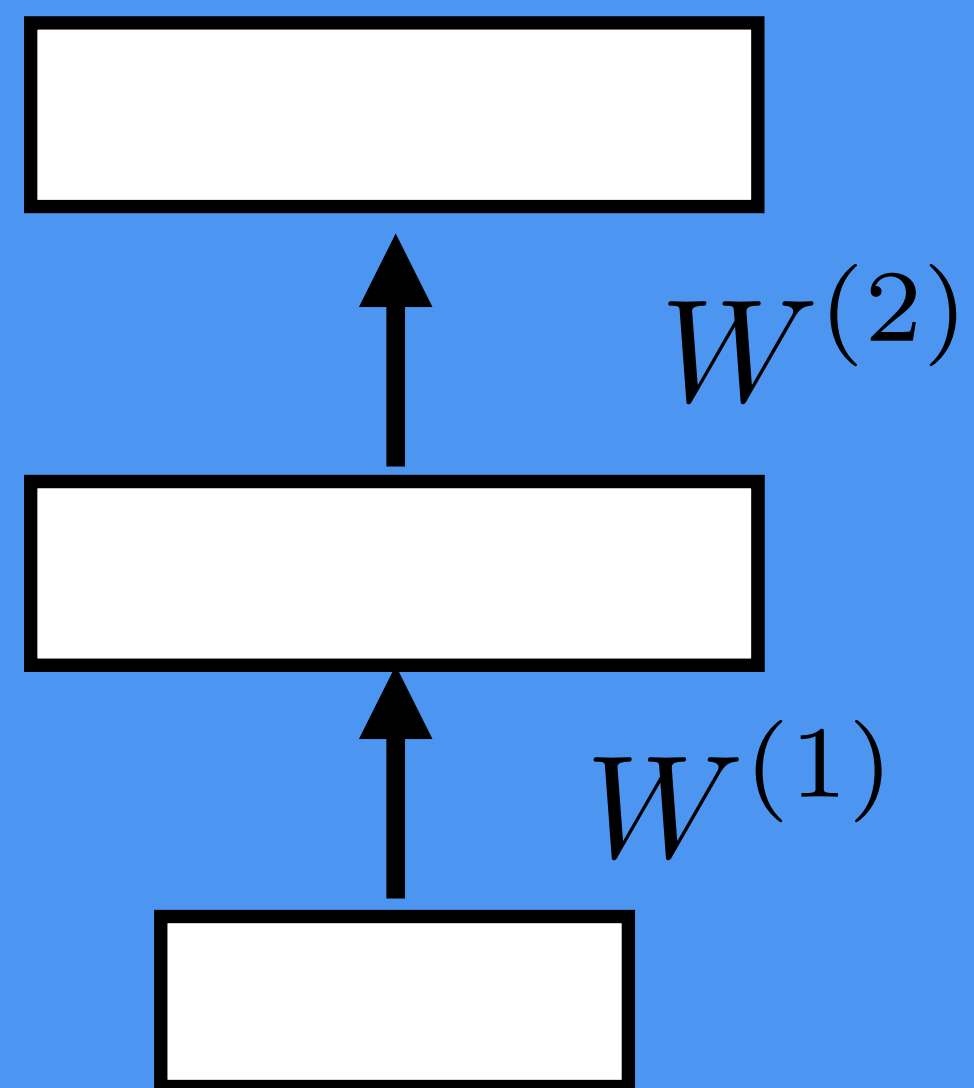
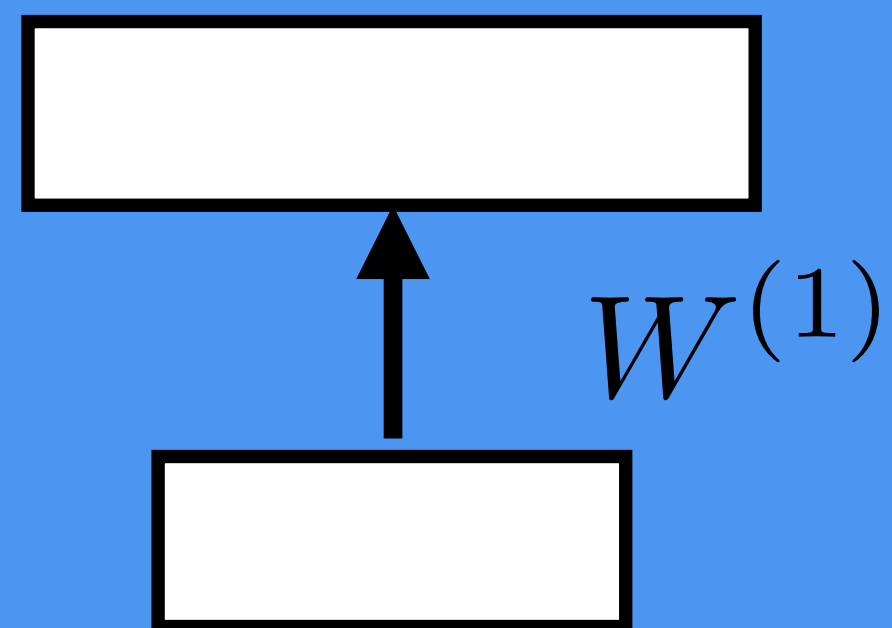
$$\tau_L \frac{dW_{\mu i}}{dt} = g(h_\mu) \left[v_i - \left(\sum_{k=1}^N W_{\mu k} v_k \right) W_{\mu i} \right]$$

$$\sum_{i=1}^N W_{\mu i}^2 = 1$$

The weights of each hidden unit dynamically converge to the surface of a unit sphere

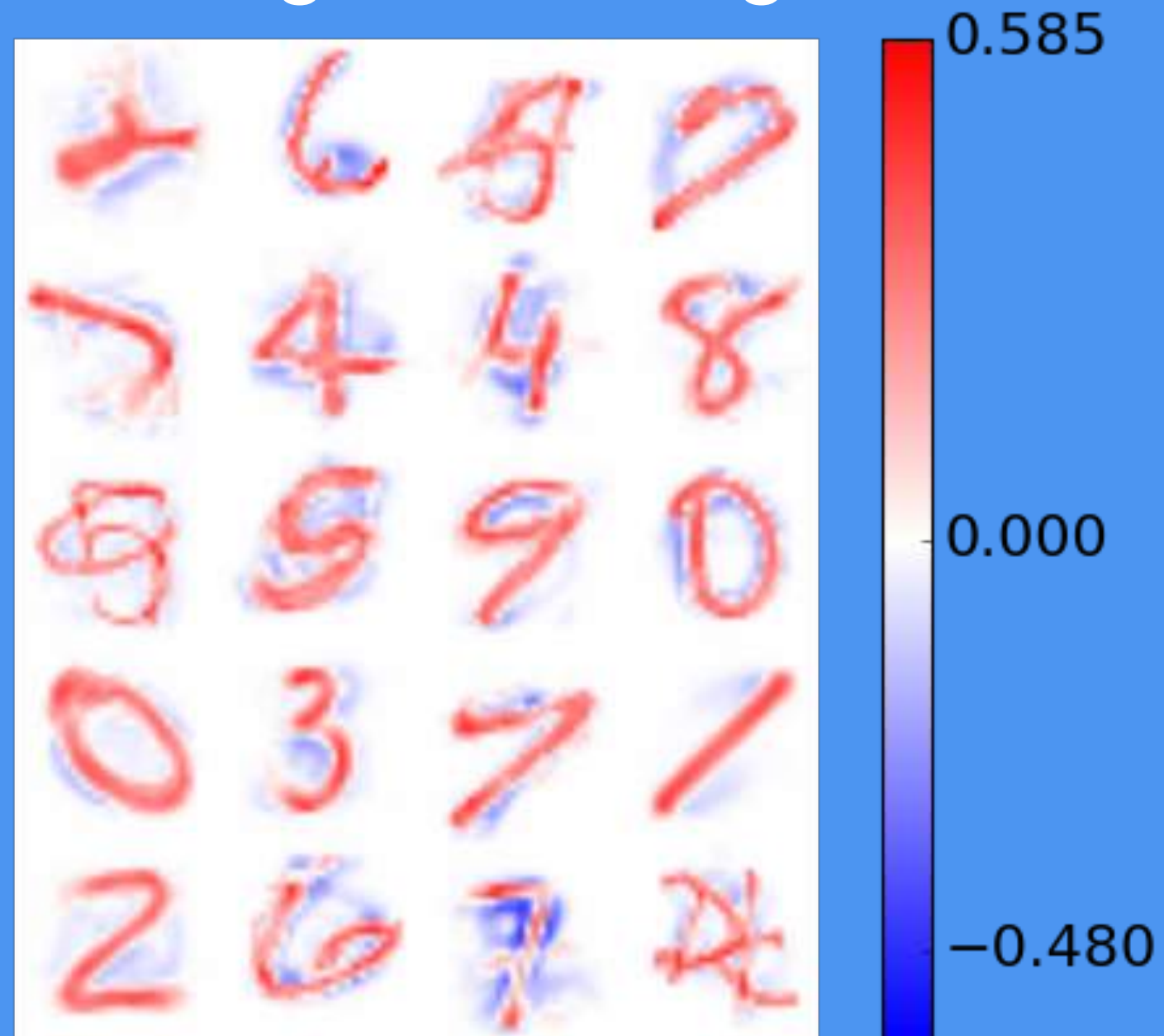


Stacking the layers

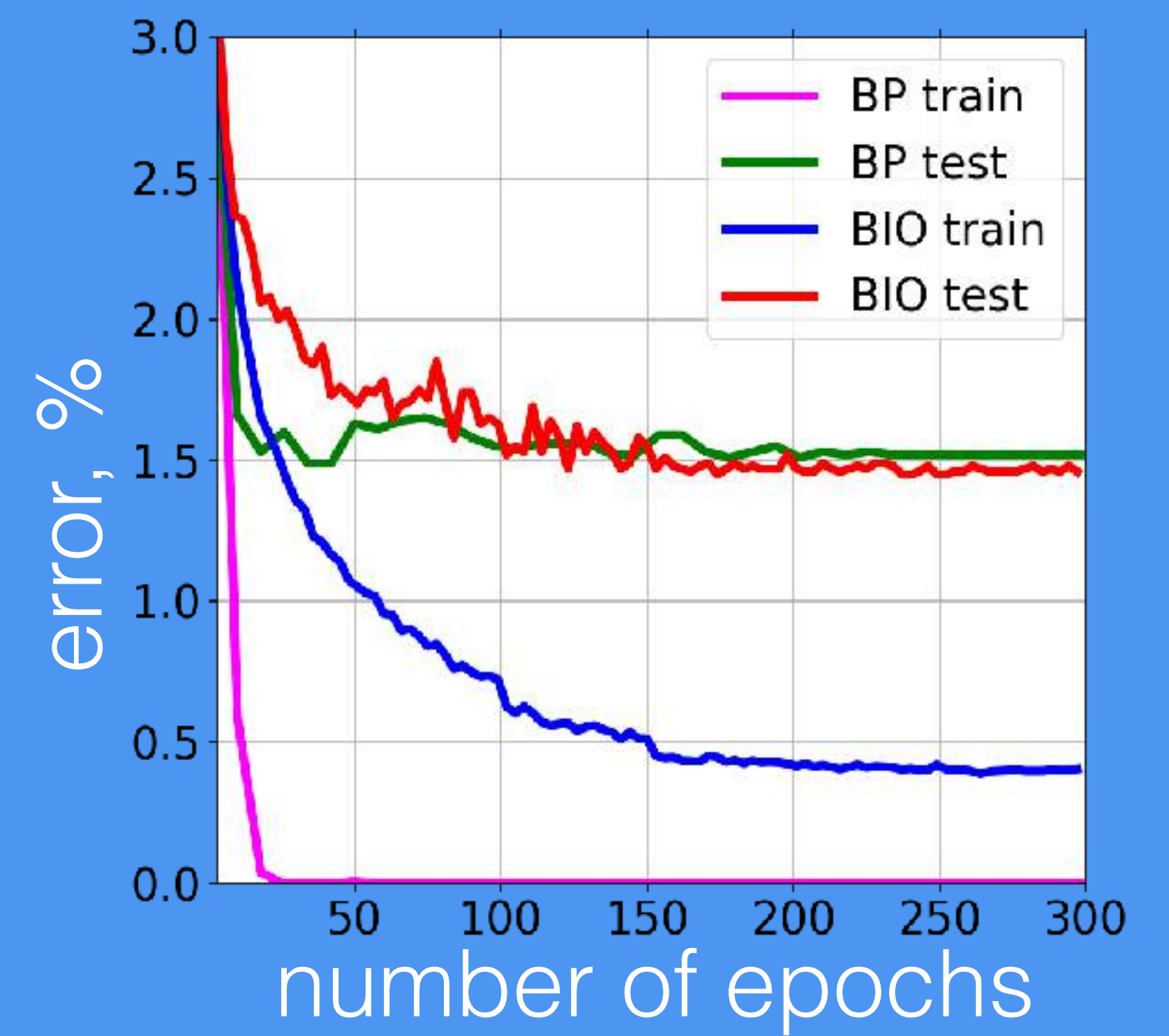
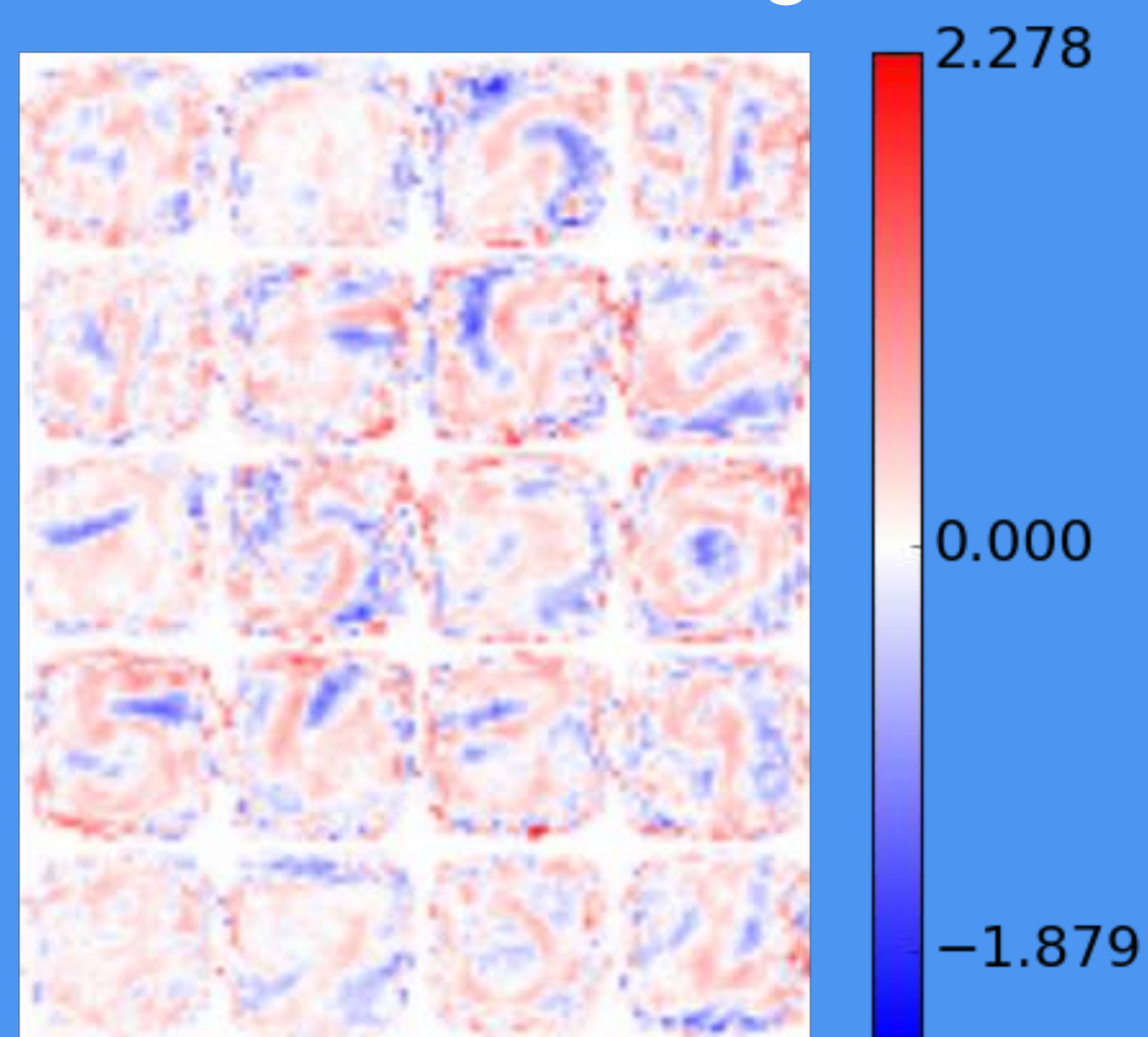


Generalization performance

“biological training”



end-to-end training



Alternative ideas on biologically plausible learning



test error = 2-3%

Equilibrium Propagation: Bridging the Gap between Energy-Based Models and Backpropagation

Benjamin Scellier* and Yoshua Bengio†

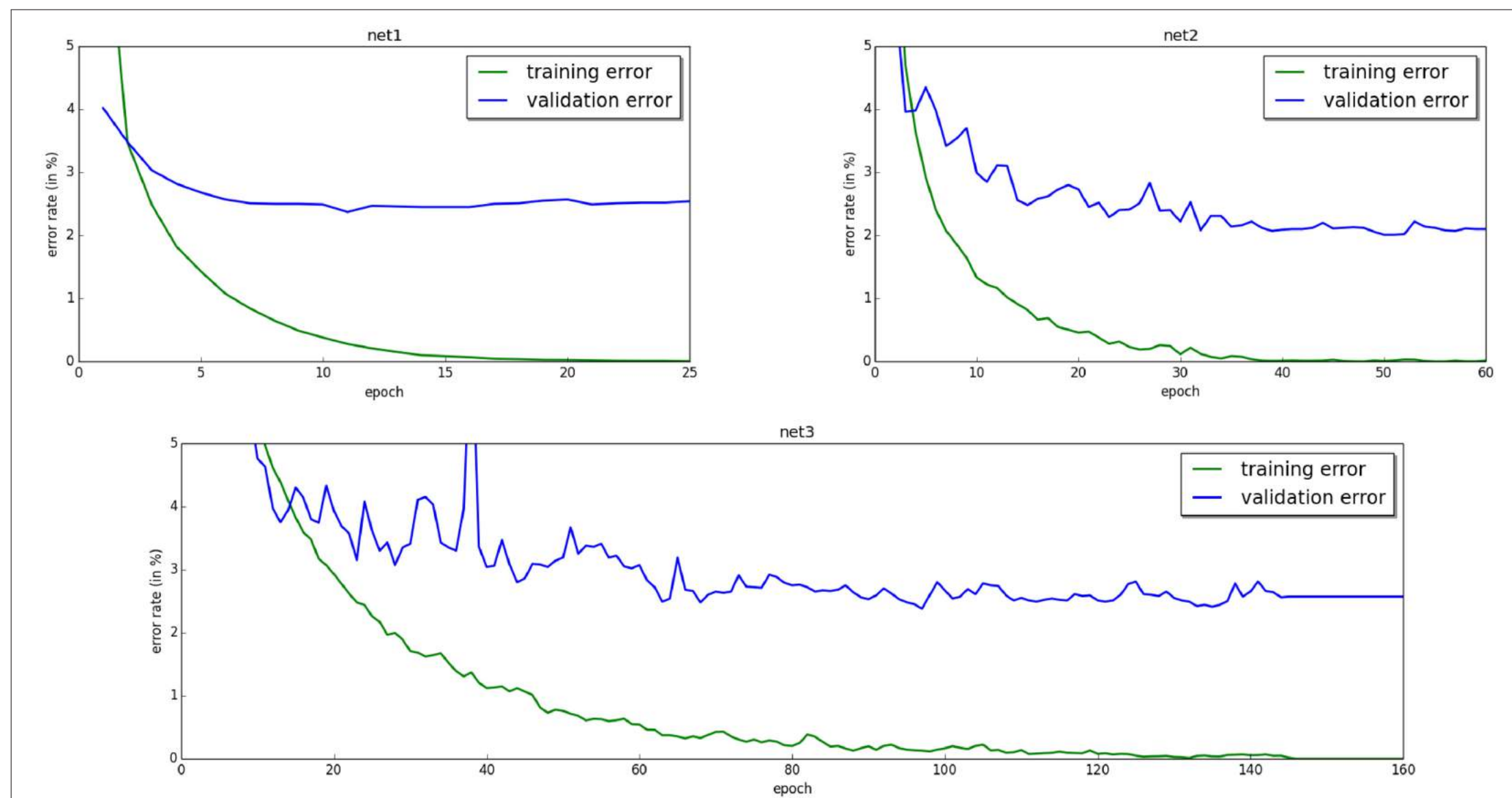


FIGURE 3 | Training and validation error for neural networks with one hidden layer of 500 units (top left), two hidden layers of 500 units (top right), and three hidden layers of 500 units (bottom). The training error eventually decreases to 0.00% in all three cases.

Dendritic error backpropagation in deep cortical microcircuits

João Sacramento^{1*}, Rui Ponte Costa¹, Yoshua Bengio², Walter Senn^{1*}

¹Department of Physiology
University of Bern, Switzerland

²Montreal Institute for Learning Algorithms
Université de Montréal, Québec, Canada

test error = 1.96%

Abstract

Animal behaviour depends on learning to associate sensory stimuli with the desired motor command. Understanding how the brain orchestrates the necessary synaptic modifications across different brain areas has remained a longstanding puzzle. Here, we introduce a multi-area neuronal network model in which synaptic plasticity continuously adapts the network towards a global desired output. In this model synaptic learning is driven by a local dendritic prediction error that

30 Dec 2017

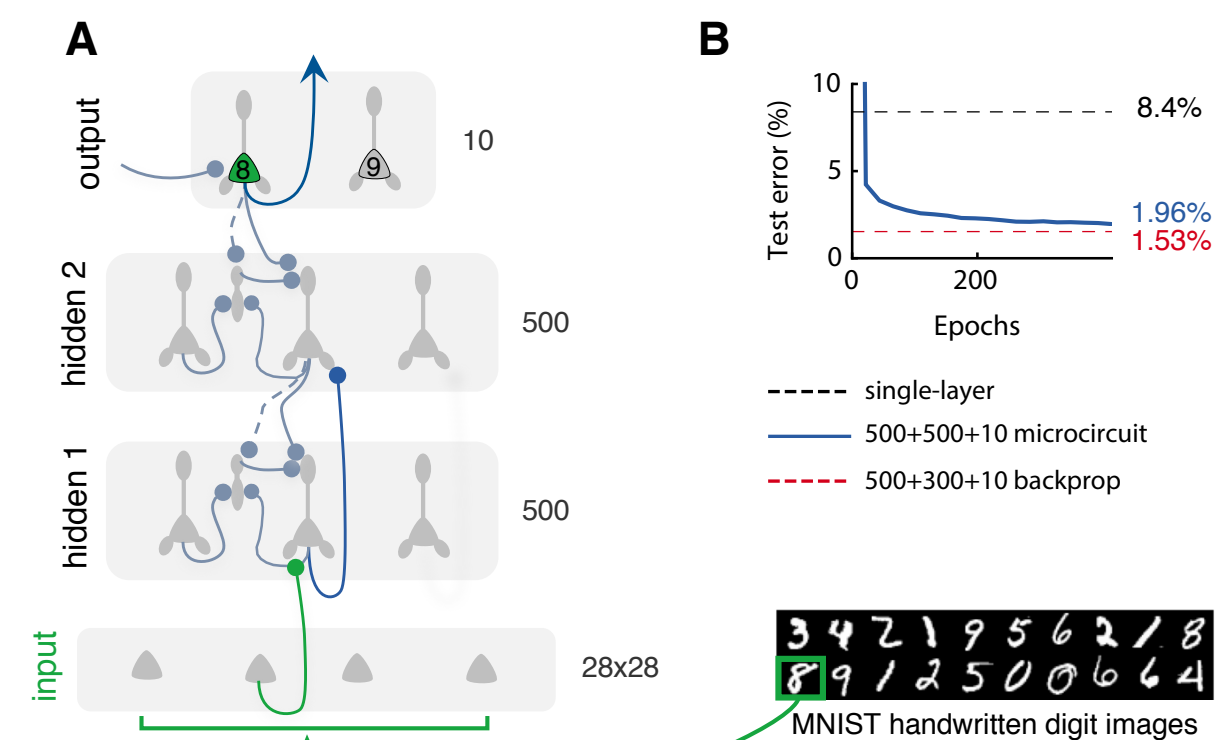
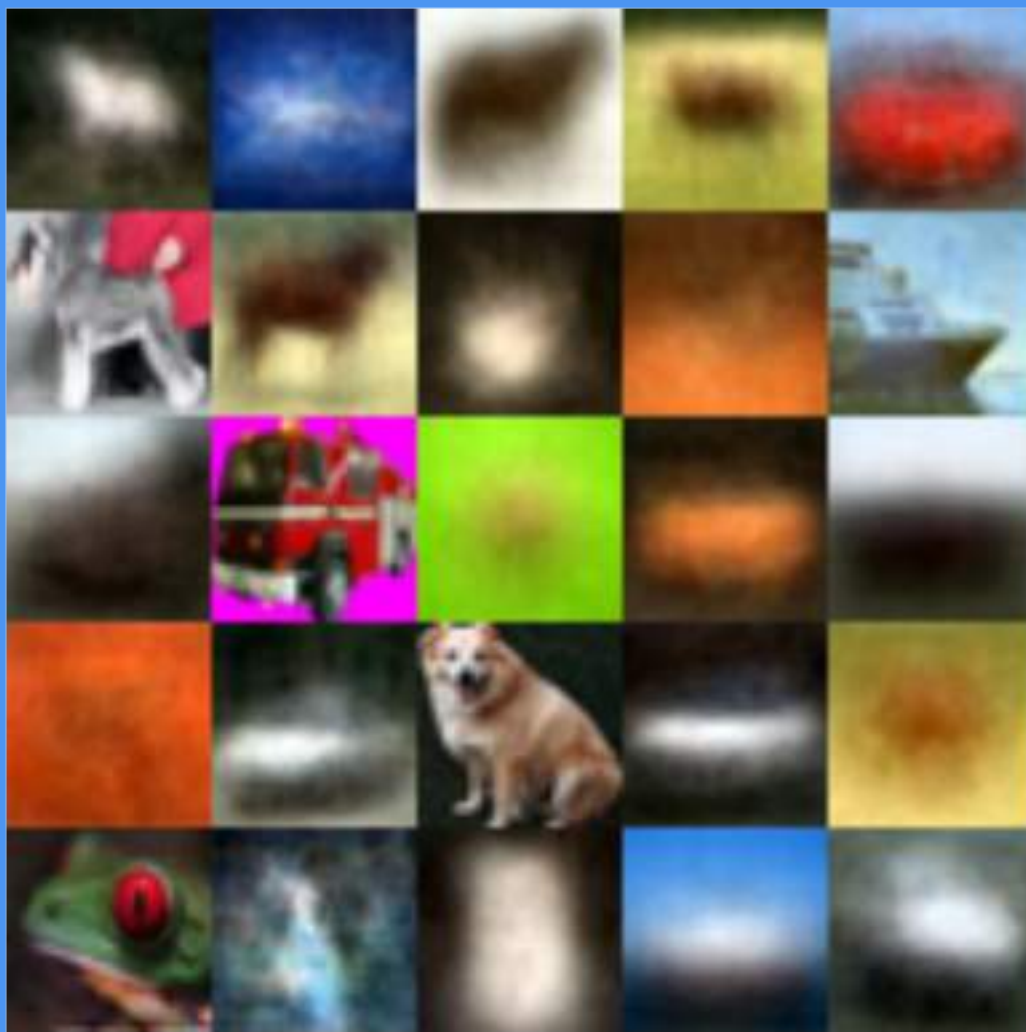


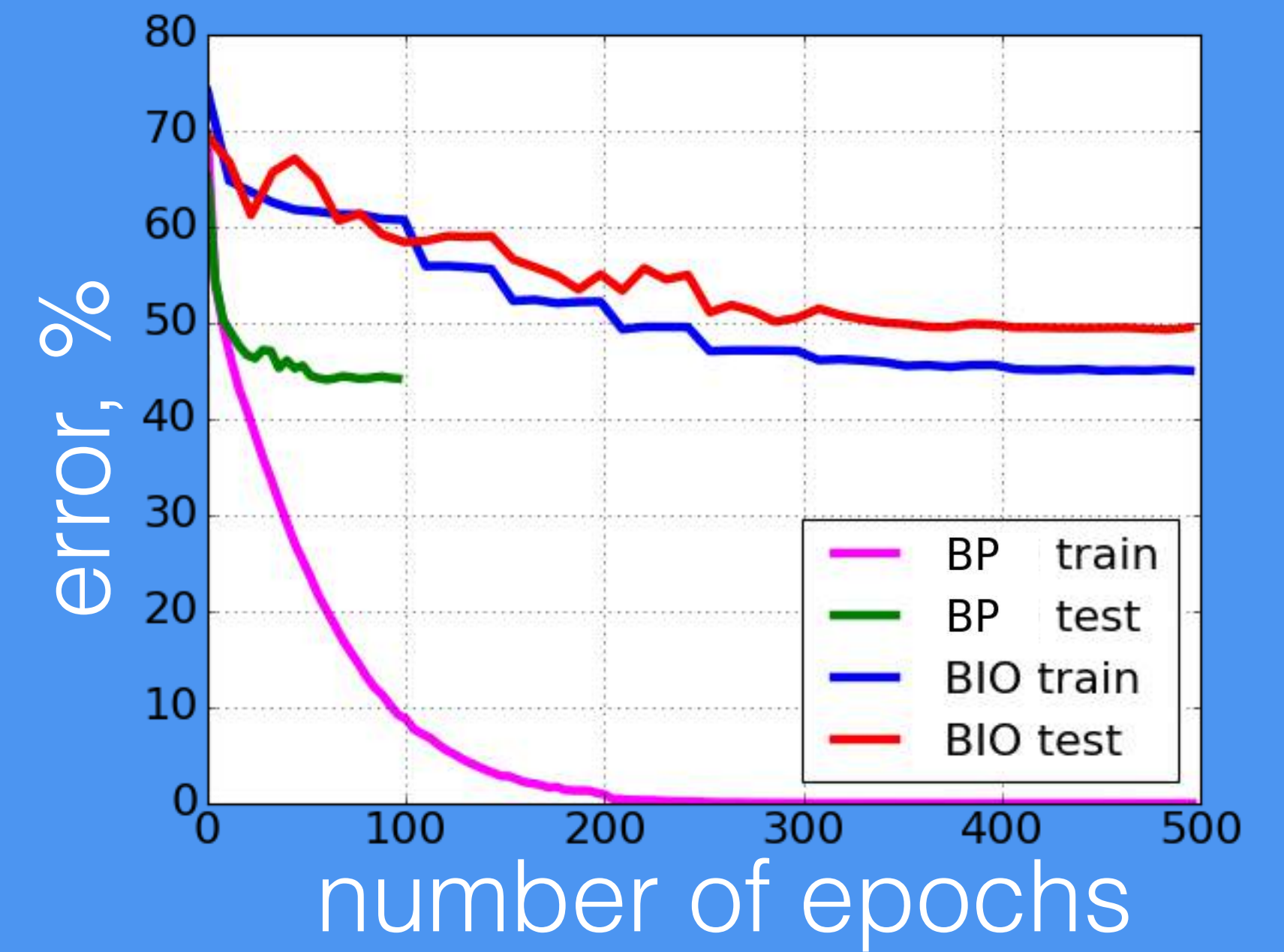
Figure 4: **Learning to classify real-world, structured stimuli with a multi-area network.** (A) A 784-500-500-10 (i.e. with two hidden areas) network of pyramidal neurons learns to recognize and classify handwritten digits from the MNIST data set. Only a subset of connections is shown to enhance clarity. (B) Competitive accuracy ($< 2\%$, an empirical signature of backprop-like learning) is achieved on the standard MNIST testing dataset by our network (solid blue). For comparison the performance of a shallow learner (i.e. a network in which only output weights are adapted, dashed black) and of a standard artificial neural network trained with backprop (dashed red, see Methods) are also shown.

Generalization performance on CIFAR-10

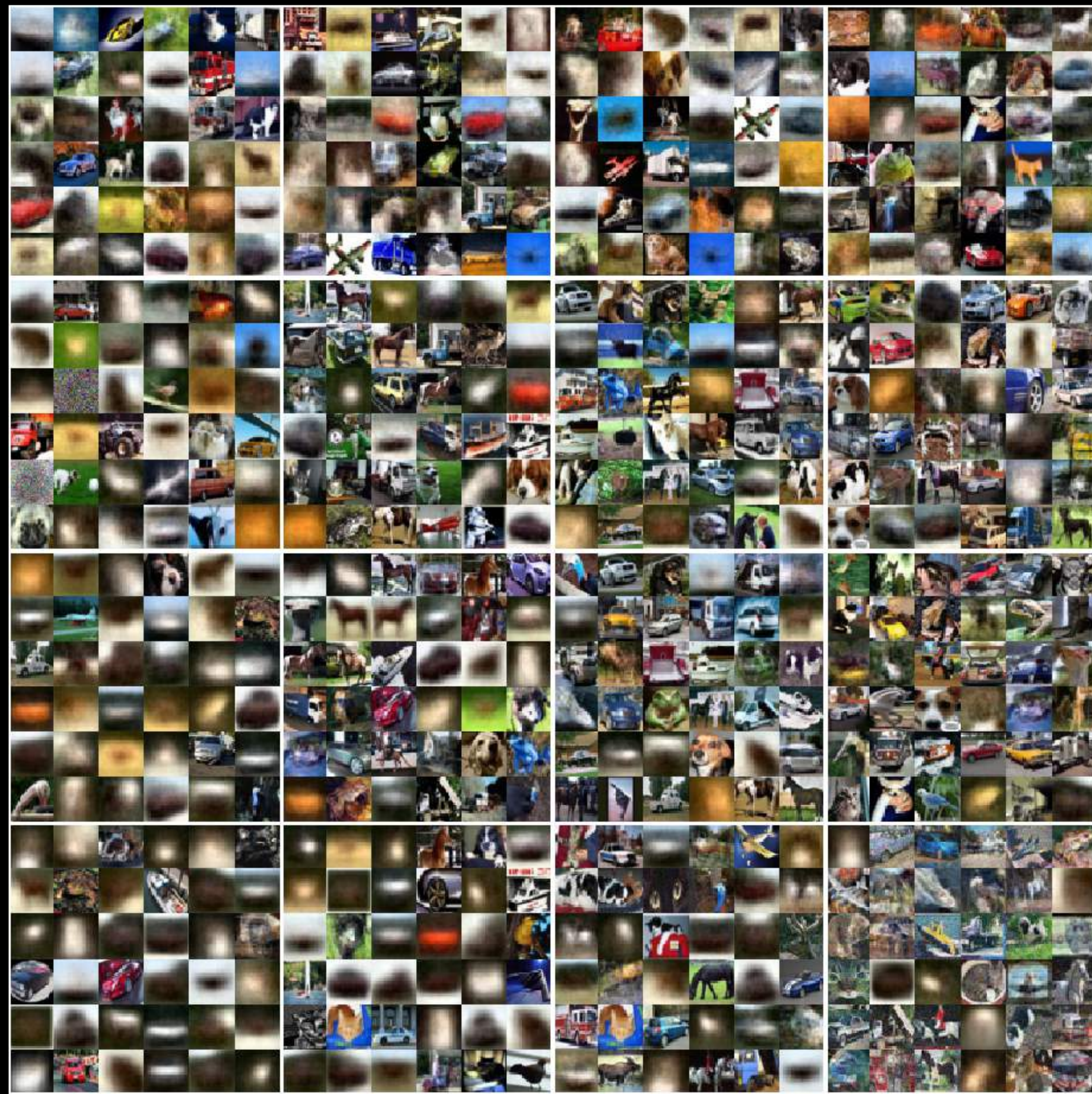
“biological training”



end-to-end training



Lebesgue norm p



$p=2$

$p=3$

$p=4$

$p=5$

Strength of anti-hebbian learning



Work with L. Grinberg

Conclusions

1. Generalization performance of the “biologically plausible” neural network is close to that of the neural network trained end-to-end.
2. The weights of the intermediate layers $W^{(1)}$, $W^{(2)}$, etc., do not have information about the task the network will have to solve eventually. Thus, they produce a “general” representation of the data.

D.Krotov, J.Hopfield: “Unsupervised learning by competing hidden units”,
arXiv:1806.10181



github.com/DimaKrotov/Biological_Learning

Twitter:

@dimakrotov